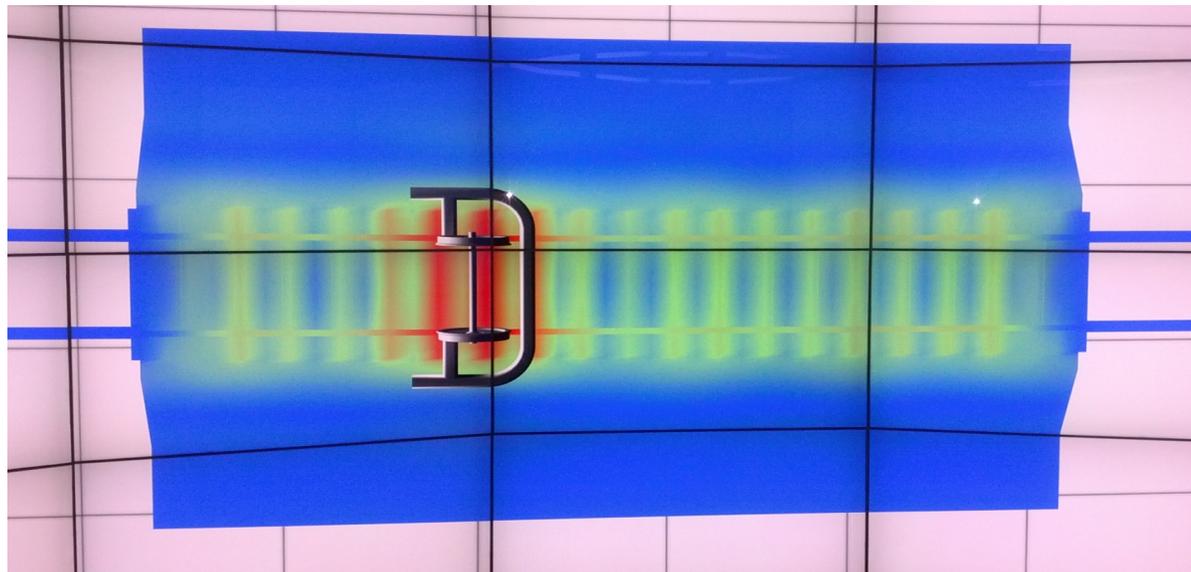


Coupled Multibody and Finite Element Modeling for Simulating Vehicle-Track-Substructure Interaction



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Dynamics Laboratory

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Rail substructure is essential for performance

Ballast, subballast, and subgrade:

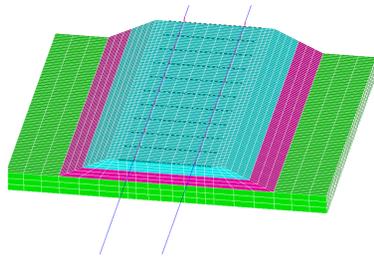
- Support track structure
- Provide drainage
- Damp track vibrations

Some potential issues

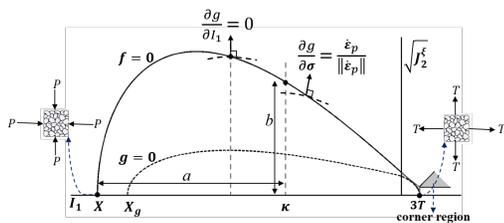
- Differential settlement, especially at transitions
- Increased maintenance
- Passenger comfort
- Vibrations in nearby structures



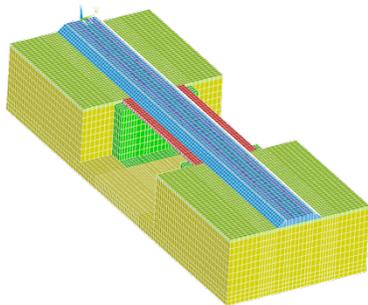
Outline



Elastic soil coupling with Rail Multibody Simulation

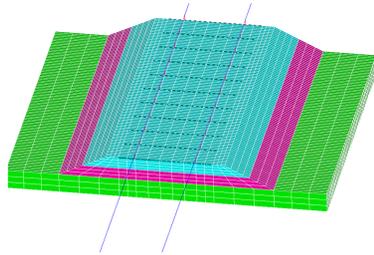


Elasto-viscoplastic soil model

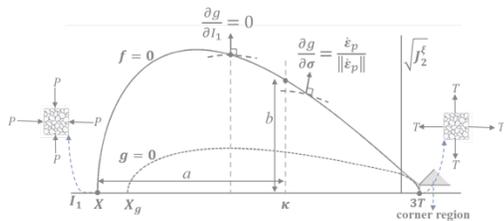


Ongoing work

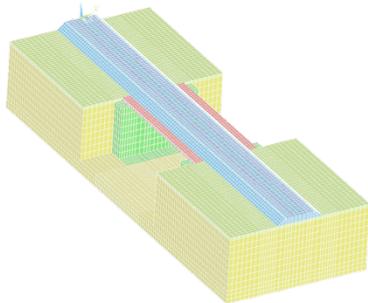
Outline



Elastic soil coupling with Rail Multibody Simulation



Elasto-viscoplastic soil model

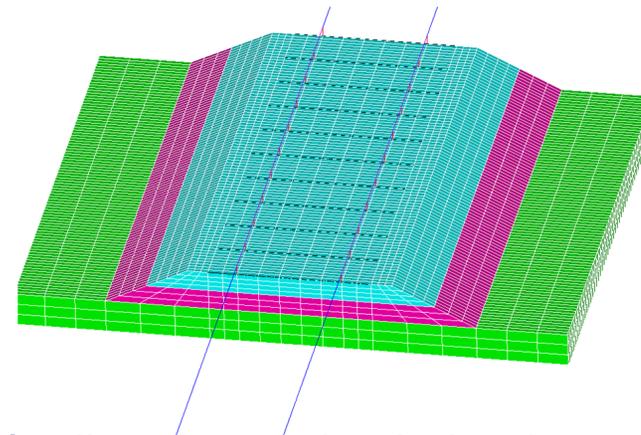
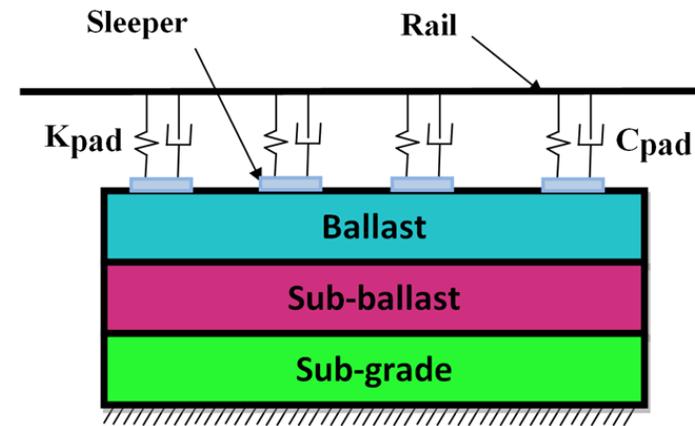


Ongoing work

Elastic modeling of soil can simulate dynamic response of track substructure

Coupling procedure

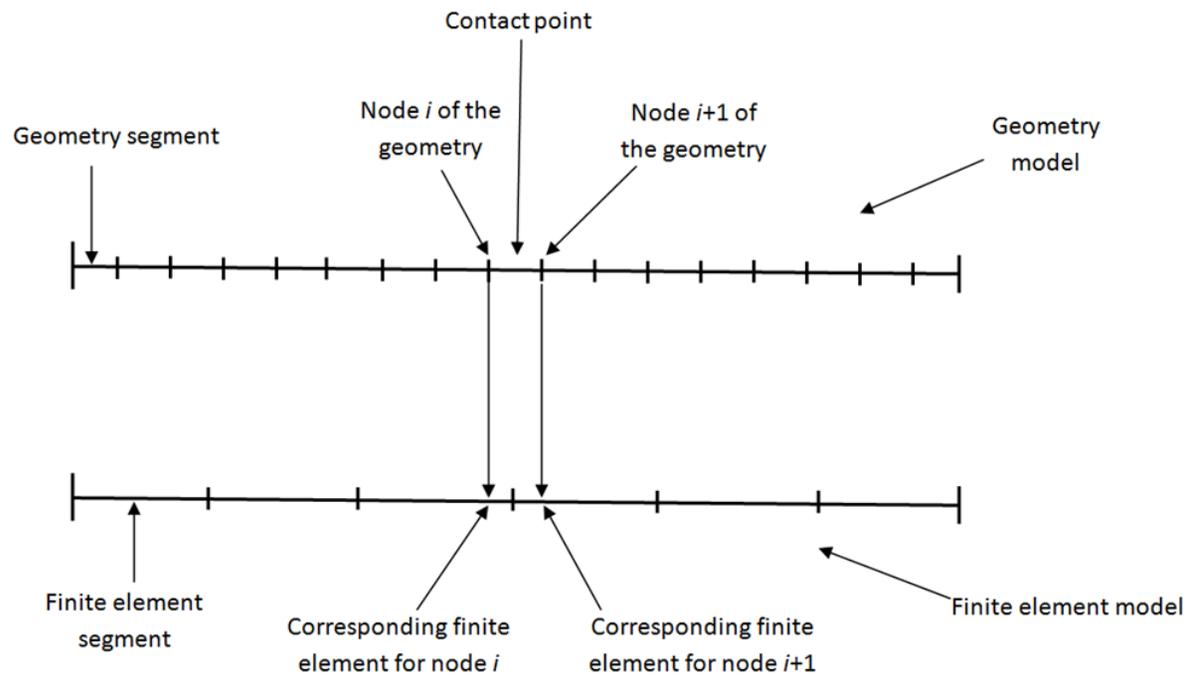
- Construct geometric model of track and substructure
- Create finite element discretization to find mass and stiffness matrices
- Extract relevant mode shapes, modal mass and stiffness
- Use mass and stiffness values to run multibody simulation of train
- Reconstruct total deformation and other quantities of interest



Run time depends on number of modes and rail nodes, not substructure geometry

Wheel-rail contact calculated in SAMS/rail

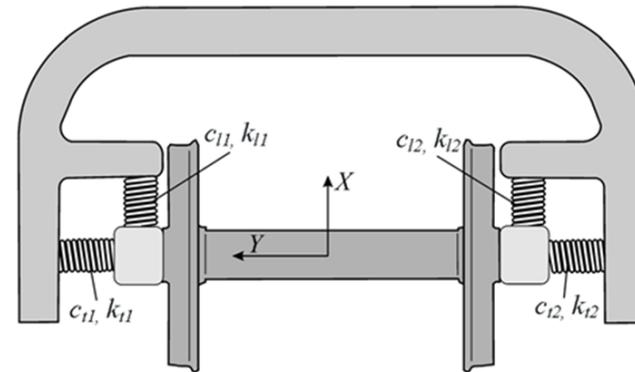
- Multibody dynamics code calculates dynamic interaction or rigid and flexible bodies coupled by algebraic constraints
- SAMS/rail includes sophisticated calculation of wheel-rail contact points and forces



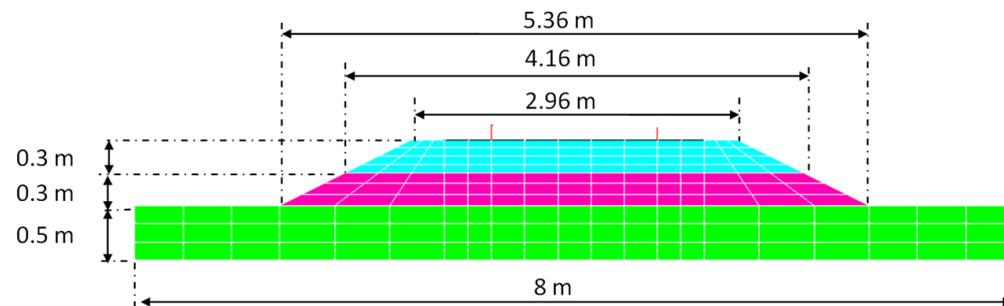
Example - suspended wheelset on elastic soil

Wheelset:

Mass	1568 kg
I_{xx}	656 kgm ²
I_{yy}	168 kgm ²
I_{zz}	656 kgm ²
$k_{11} = k_{12}$	13,500 N/m
$k_{t1} = k_{t2}$	25,000 N/m
$c_{11} = c_{12}$	1000 Ns/m
$c_{t1} = c_{t2}$	0 Ns/m



Substructure Geometry:



Example - suspended wheelset on elastic soil

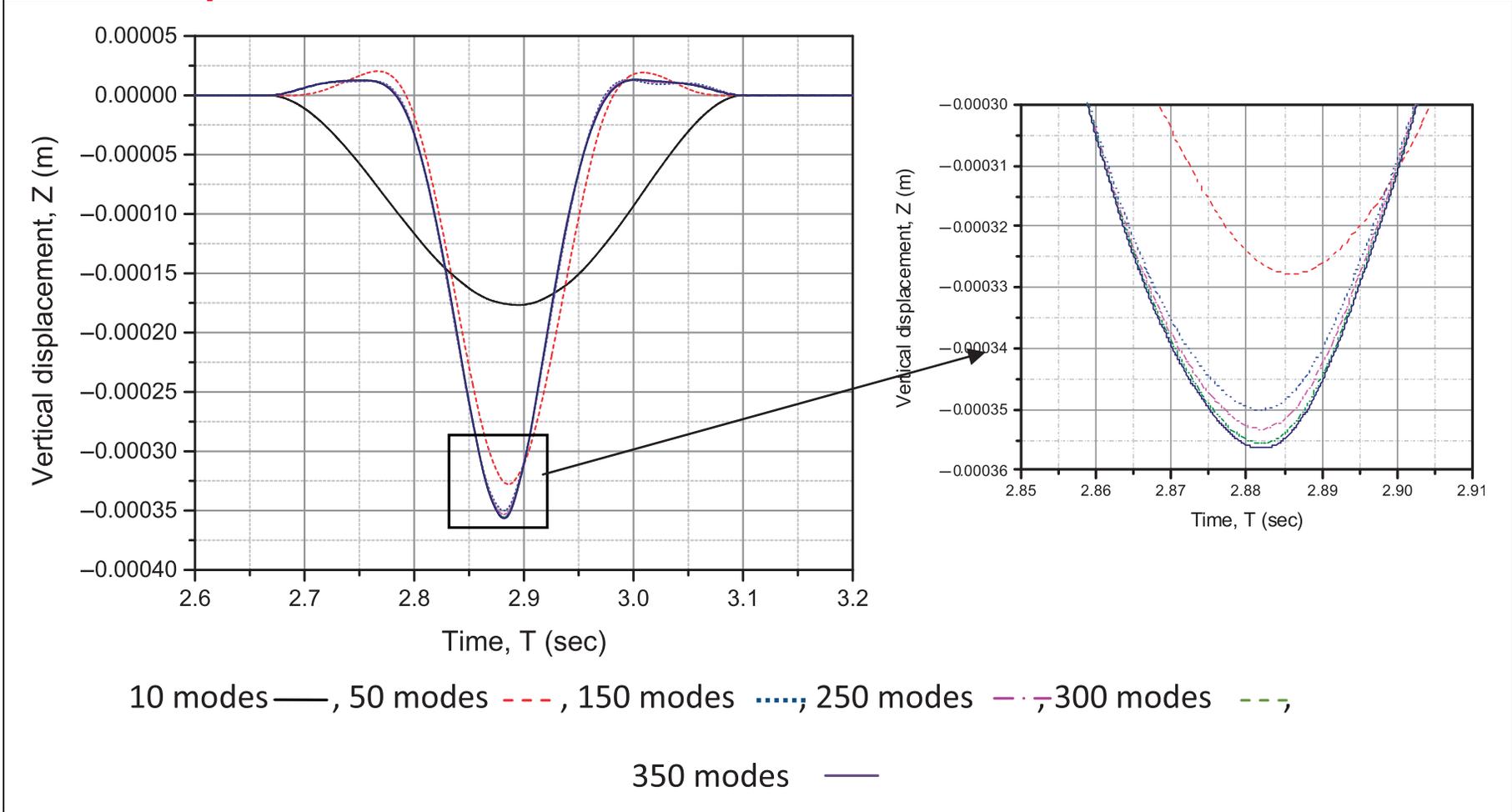
Rail and substructure parameters

Rigid rail length	40 (on both sides)	m	Poisson's ratio of a sleeper (ε_s)	0.25	
Gage length	1.5113	m	Cross-sectional area of a sleeper (A_s)	513.8×10^{-4}	m^2
Flexible rail length	6.5	m	Second moment of inertia of a sleeper, I_{yy}	$25,735 \times 10^{-8}$	m^4
Stiffness of the rail (E_r)	210×10^9	N/m^2	Second moment of inertia of a sleeper, I_{yy}	$18,907 \times 10^{-8}$	m^4
Density of the (ρ_r)	7700	kg/m^3	Timoshenko shear coefficient of a sleeper	0.83	
Poisson's ratio of the rail (ε_r)	0.3		Stiffness of the ballast (E_b)	260×10^6	N/m^2
Cross-sectional area of the rail (A_r)	64.5×10^{-4}	m^2	Density of the ballast (ρ_b)	1300	kg/m^3
Second moment of inertia of the rail, I_{yy}	2010×10^{-8}	m^4	Poisson's ratio of the ballast (ε_b)	0.3	
Second moment of inertia of the rail, I_{zz}	326×10^{-8}	m^4	Stiffness of the sub-ballast (E_{sb})	200×10^6	N/m^2
Timoshenko shear coefficient for the rail	0.34		Density of the sub-ballast (ρ_{sb})	1850	kg/m^3
Length of a sleeper	2.36	m	Poisson's ratio of the sub-ballast (ε_{sb})	0.35	
Gap between sleepers	0.65	m	Stiffness of the sub-grade (E_{sg})	200×10^6	N/m^2
Stiffness of a sleeper (E_s)	64×10^9	N/m^2	Density of the sub-grade (ρ_{sg})	1850	kg/m^3
Density of a sleeper (ρ_s)	2750	kg/m^3	Poisson's ratio of the sub-grade (ε_{sg})	0.3	
Stiffness coefficient of a pad (K_{pad})	26.5×10^7	N/m	Damping coefficient of the pad (C_{pad})	4.6×10^4	Ns/m

Results can be visualized with help from Electronic Visualization Laboratory



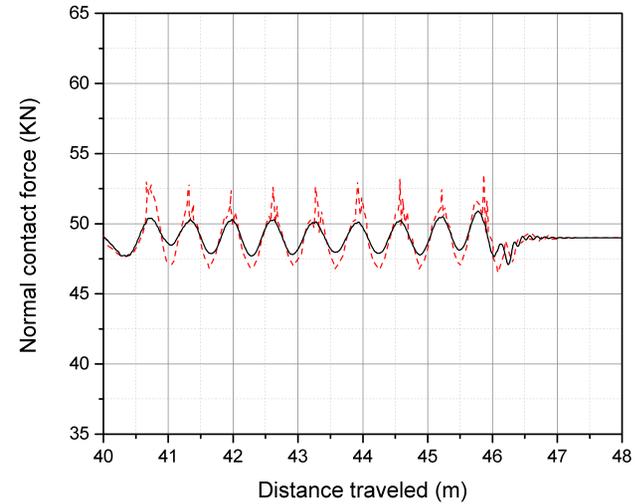
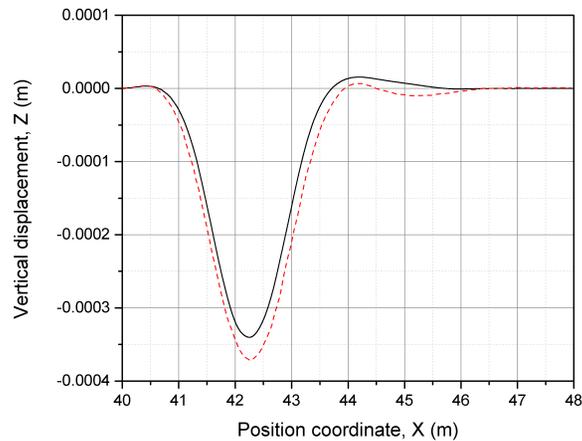
Displacement of rail can be calculated



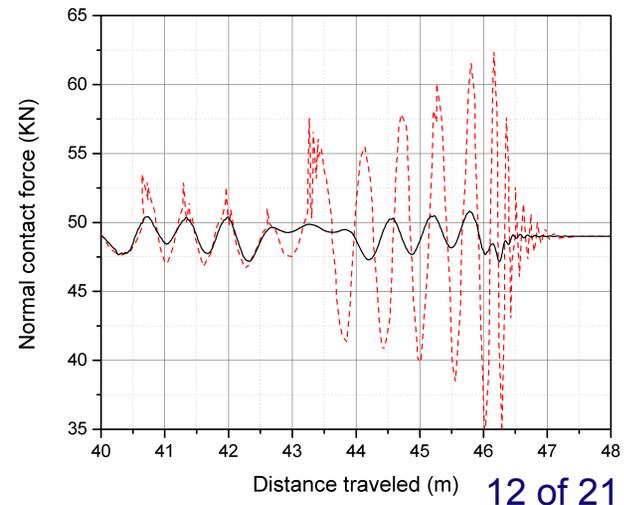
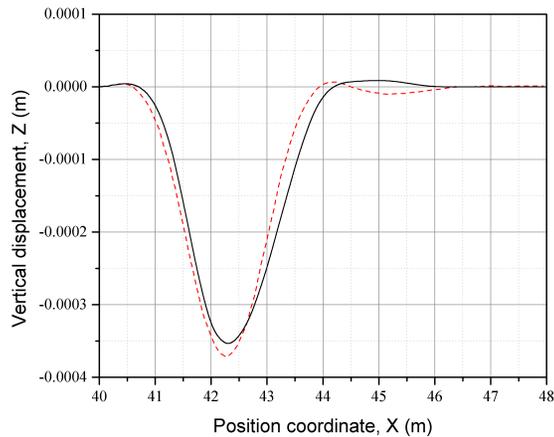
Many modes are necessary for accurate solution of a concentrated, moving load.

Results can be compared for “normal” track and unsupported tie

Normal rail displacement and contact force between ties



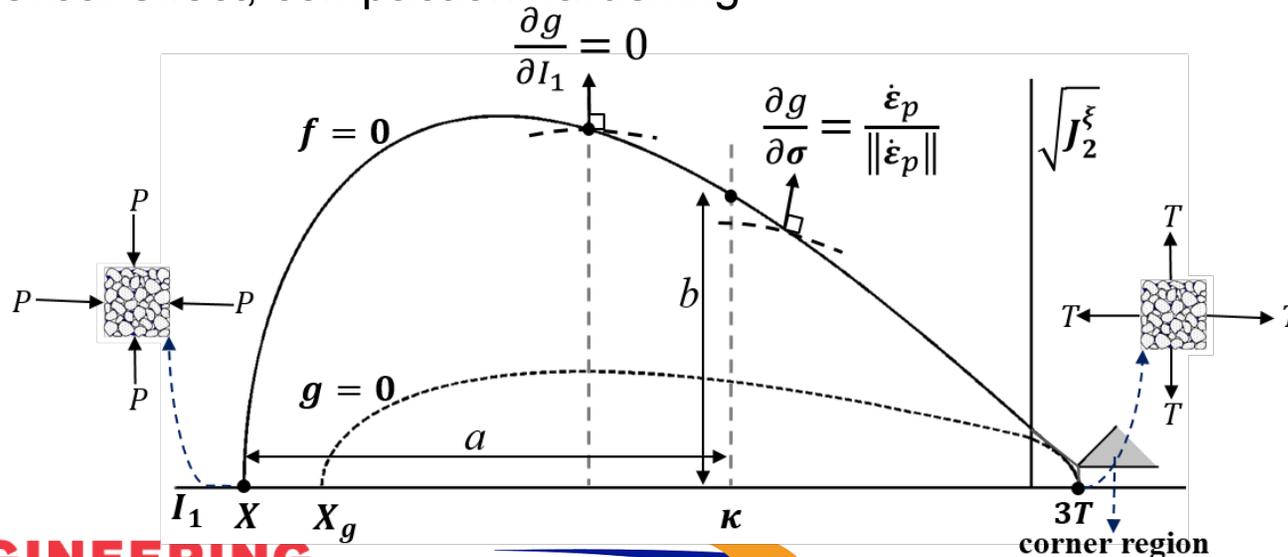
Rail displacement for unsupported tie



Permanent deformation requires inelastic modeling

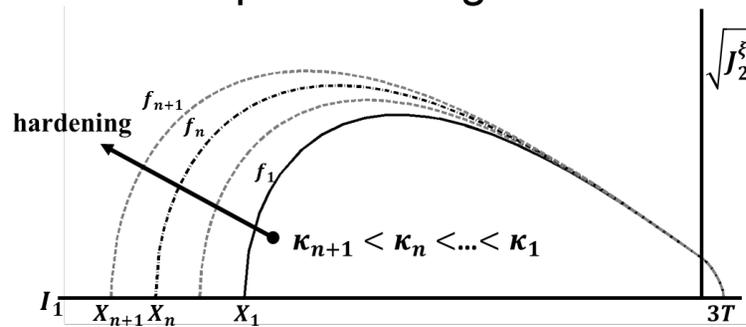
Important features for ballast, subballast and subgrade settlement:

- Dilation at low pressure, compaction higher
- Rate dependence
- Kinematic hardening to capture Bauschinger effect in cyclic loading
- Other features for improved accuracy: nonassociativity, strength differential effect, compaction hardening

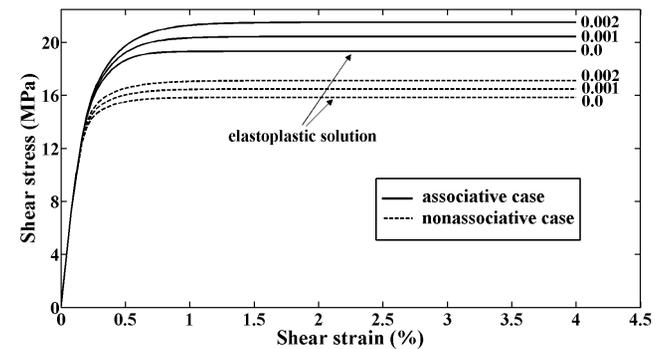


We have adapted the Sandia GeoModel, a cap plasticity model, to capture these features.

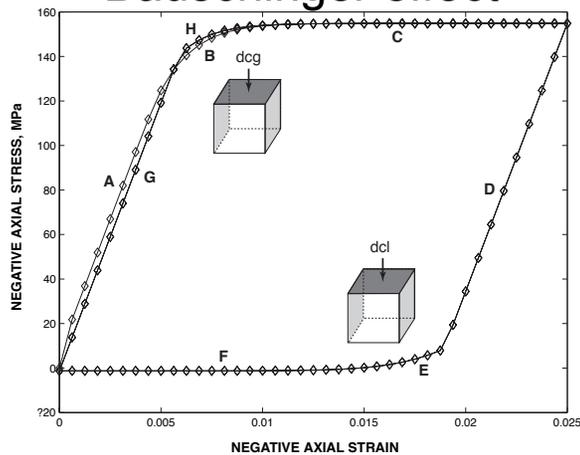
Cap hardening



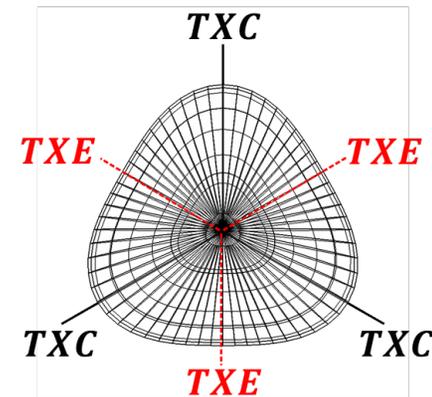
Rate dependence



Bauschinger effect



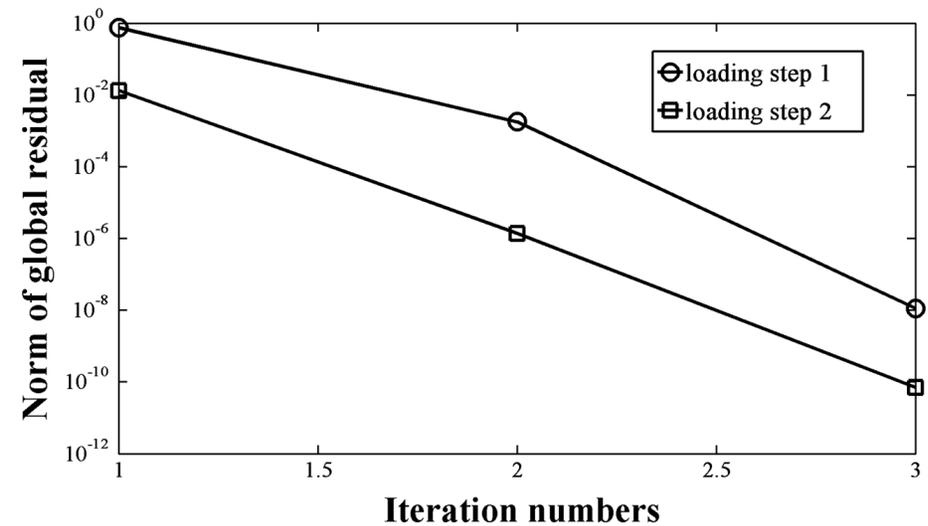
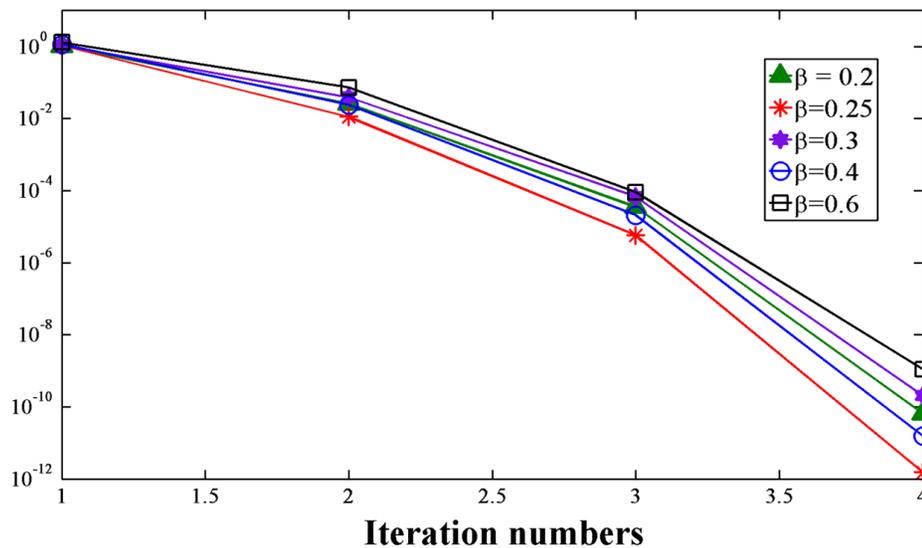
Strength differential



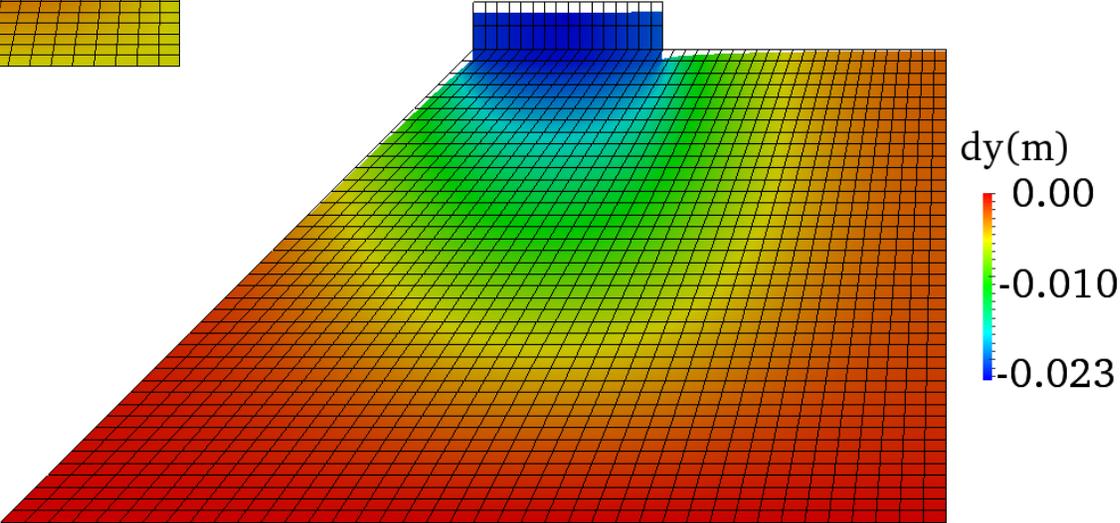
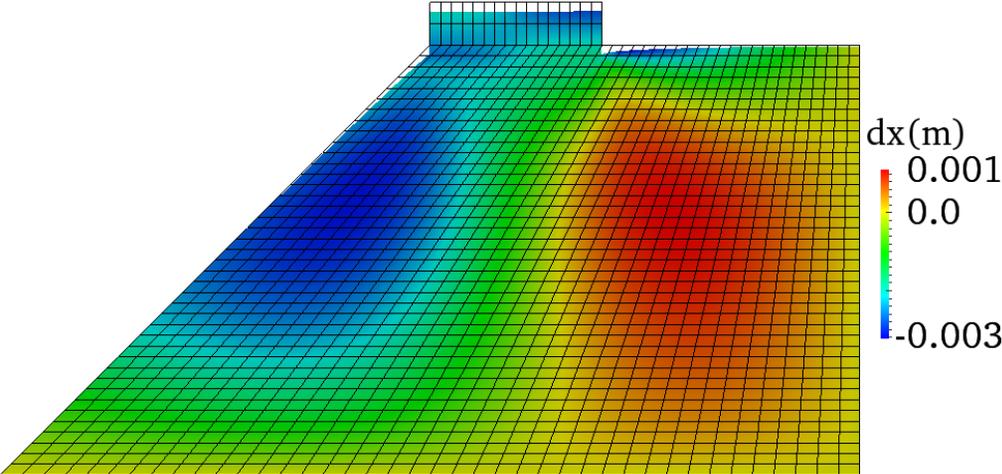
Recent modifications have improved robustness and efficiency

- Reparameterized yield function
- Normalized units of local residual

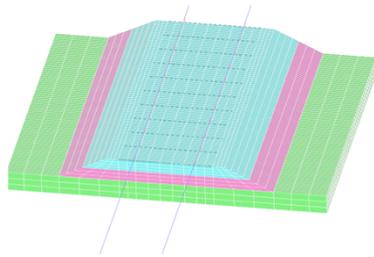
Both local and global residuals show quadratic convergence



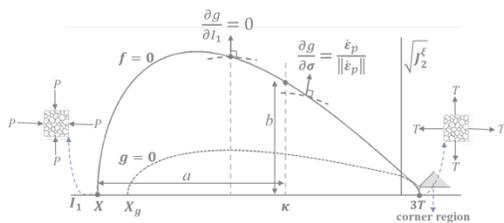
The model can be used in large-scale finite element problems



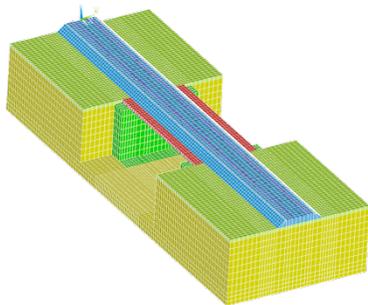
Outline



Elastic soil coupling with Rail Multibody Simulation

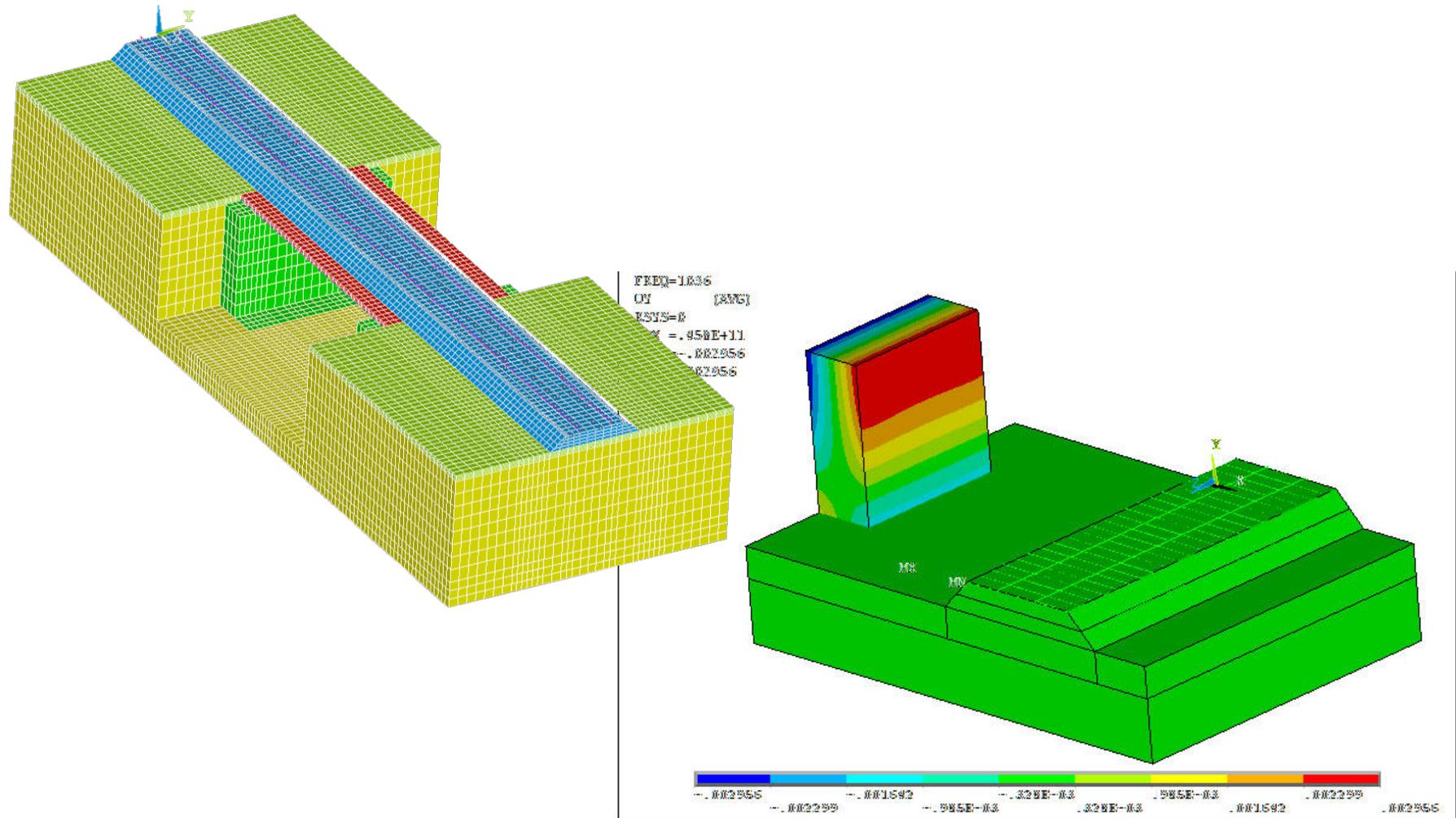


Elasto-viscoplastic soil model



Ongoing work

This linear elastic model is now being applied to bridge approaches and building vibrations



This viscoplastic model will be coupled to the multibody model by a linear approximation

- Use linear stiffness to calculate displacements
- Use the displacement to calculate full stress and plastic strain
- Since inelastic deformation is small over a given event, rerun loads
- Periodically update geometry to account for settlement

Conclusions

- Continuum modeling of track substructure lead to more accurate modeling of train dynamics
- Can be applied to a variety of problems related to rail geotechnics, including building vibration and transitions
- More advanced soil modeling necessary to capture permanent settlement (ballast fouling and degradation needs further modification)

References

- [1] Motamedi, M. H., Foster, C. D., (2015), "An improved implicit numerical integration of a non-associated, three-invariant cap plasticity model with mixed isotropic/kinematic hardening for geomaterials" *IJNAMG*, In Press.
- [2] El-Ghandour, Ahmed I., Martin B. Hamper, and Craig D. Foster. "Coupled finite element and multibody system dynamics modeling of a three-dimensional railroad system." *JRRT* (2014): 0954409714539942.
- [3] Recuero, A. M., J. L. Escalona, and A. A. Shabana. "Finite-element analysis of unsupported sleepers using three-dimensional wheel–rail contact formulation." *JMD* 225.2 (2011): 153-165.
- [4] C.D. Foster, R.A. Regueiro, A.F. Fossum, and R.I. Borja. (2005), "Implicit numerical integration of a three-invariant, isotropic/kinematic hardening cap plasticity model for geomaterials" *CMAME*, Vol. 194, Nos. 50-52, 5109-5138.